

Channel Networks Statistics

A. Plan-form Network Properties

Dendritic channel network most common, scale-invariant.

Other forms (trellis, radial patterns, etc.) \Rightarrow lithologic and structural control.

D_d = drainage density

$$D_d = \frac{\sum l}{A} [m^{-1}]$$

$$A_c : x_c^2$$

$$\frac{1}{\lambda} : \frac{1}{2x_c} \quad \lambda = \text{spacing between channels}$$

$D_d = f(x_c) \Rightarrow$ lithology, climate, tectonics



Scaling Laws Drainage Networks

Hack's Law (1957):

Length of a channel is related to drainage area.

$$l \propto A^{0.52-0.67}$$

$$l \propto A^{0.6}$$

$$A = k_a x^h \quad x = \text{along-stream distance}$$

$$h : 1.67$$

Horton's Laws:

Numbers of channels, lengths, areas all grow in steady geometric progression.

w = order of channel

Second order channel \rightarrow two or more first order channel join

Third order channel \rightarrow two or more second order channel join

Horton's Laws

Law of Stream numbers (Bifurcation Ratio):

$$R_n = R_b = \frac{n_w}{n_{w+1}} = \text{constant} \quad (3-5) \quad 4 \quad - \quad \text{notation: (range) mode}$$

Law of Stream areas:

$$R_a = \frac{\bar{a}_{w+1}}{\bar{a}_w} = \text{constant} \quad (3-6) \quad 4$$

Law of Stream segment lengths:

$$R_l = \frac{\bar{l}_{w+1}}{\bar{l}_w} = \text{constant} \quad (1.5-3) \quad 2$$